

Small-angle scattering for structural biology—Expanding the frontier while avoiding the pitfalls

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Overview

Goal

A review intended to, “provide a road map through the small-angle scattering experiment, while also providing a set of guidelines for the critical evaluation of scattering data.

1. Basics

- What is Small Angle Scattering?
- Essential Equations
- Contrast Matching & Variation

2. Preliminary Checks

- Sample Purity & Concentration
- Blanks

3. Data Acquisition

- Effects of Radiation & Concentration
- Initial Data Inspection

4. Modeling

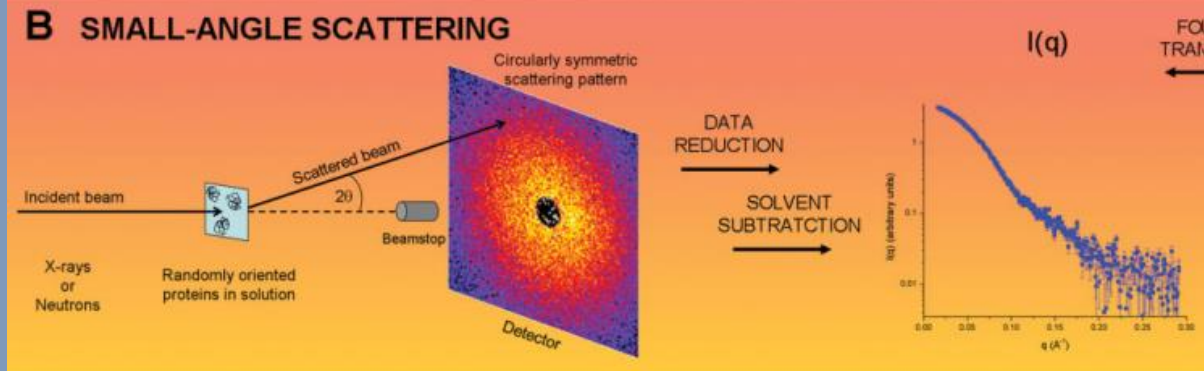
- High-Res Validation
- Multi-Domain/Subunit Modeling

Basics of SAS - What is Small Angle Scattering?

- A technique meant to provide high-precision information regarding shape and size of a molecule
- Collimated beams of x-rays or neutrons illuminate a sample, this light is scattered by the atoms of the sample
- Scattered waves are recorded by a detector
- To make sense of the data, many different forms of editing are employed

X-Ray Sample Amount:
>1mg/mL in 5-30 μ L of solution

Neutron Scattering Sample Amount:
>3mg/mL in 150-300 μ L of solution



Basics of SAS - Essential Equations

Radius of Gyration

$$R_g^2 = \frac{\int P(r)r^2 dr}{2 \int P(r)dr}$$

R_g = Radius of Gyration

$P(r)$ = Interatomic Distance
Distribution

r = Frequency of interatomic vector
lengths in a protein

Zero-Angle Scattered Intensity Equation

$$I(0) = N(\Delta\rho V)^2 = \frac{C\Delta\rho^2 v^2 M}{N_a} = 4\pi \int_0^{D_{max}} P(r)dr$$

N = Scattering particles/Unit Volume

$\Delta\rho$ = Contrast

V = Particle Volume

C = Mass/Unit Volume

v = Partial Specific Volume

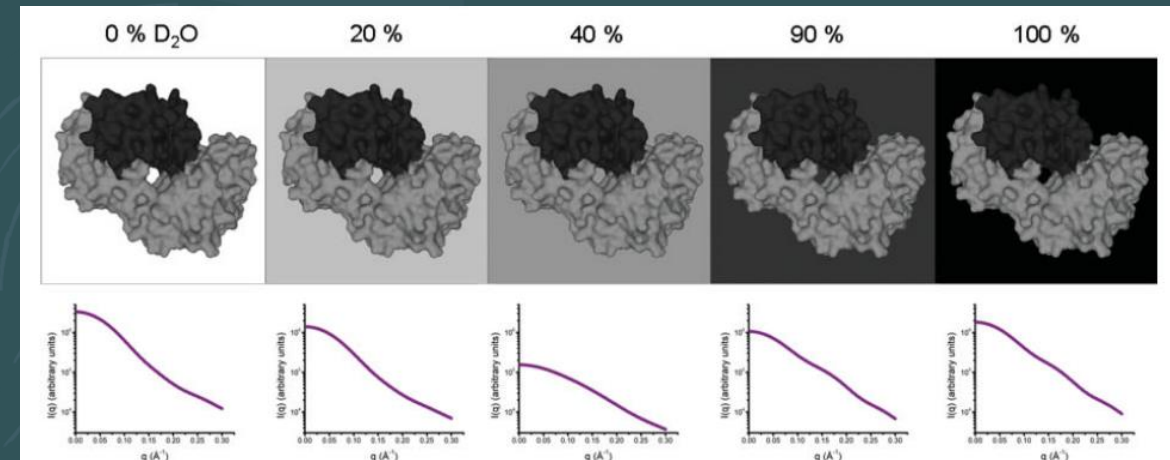
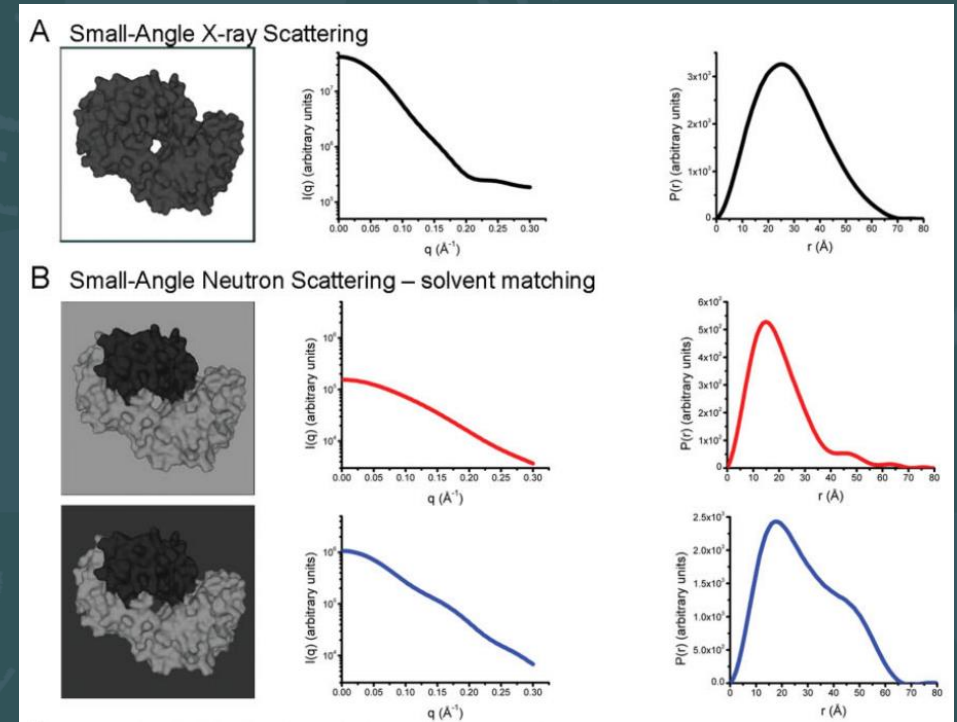
M = Molecular Weight

N_a = Avagadro's Number

D_{max} = Maximum Linear Distance

Basics of SAS - Contrast Matching & Variation

- Used primarily in molecular shape studies
- Involves the manipulation of protein and solvent scattering densities
- X-rays vs Neutrons?



Graphs: X-axis = $q(\text{\AA})$, Y-axis = $I(q)$

Preliminary Checks

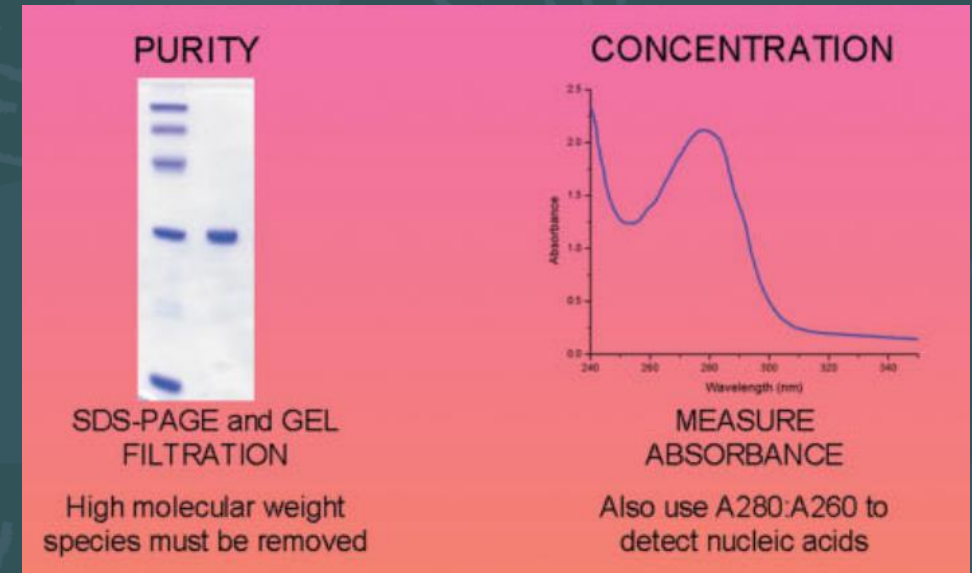
Purity, Monodispersity, & Concentration

- SDS-PAGE
- 280:260nm Absorbance Ratio
- Dynamic Light Scattering

- SEC

Blanks

- Matching solvent blanks are needed to obtain the scattering of the protein
- Dialysis is recommended by the authors to ensure a matched blank



Data Acquisition

Radiation Damage

- Bond Breakage & Free Radical Formation
- Radiation Induced Aggregation

Solutions

- Free Radical Absorber in solvent (DTT, Ascorbate)
- Exposure and Result Comparison
- SDS-PAGE

Concentration Effects

- Looking at $I(0)/C$, C , & R_g can help deduce if there is concentration dependent interference

RADIATION DAMAGE



MEASURE TIMECOURSE

$I(0)$ and R_g should show
no time-dependence

CONCENTRATION EFFECTS



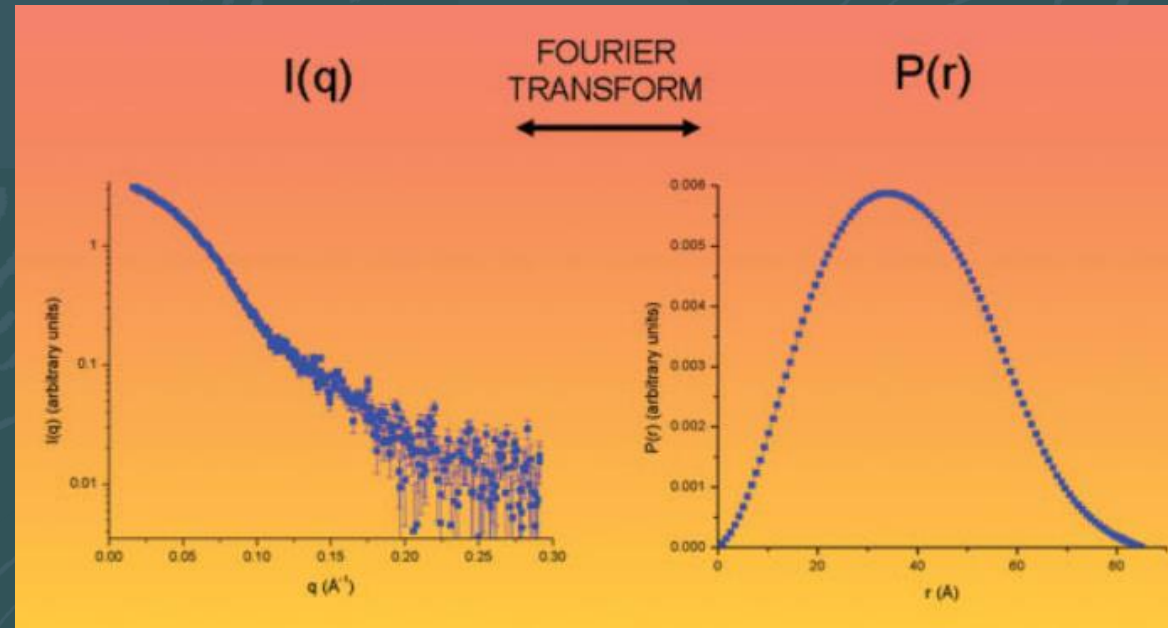
MEASURE CONCENTRATION SERIES

$I(0)/C$ and R_g should remain constant.
Increase with C indicates aggregation,
decrease indicates interparticle interference

Data Acquisition

Data Transformation

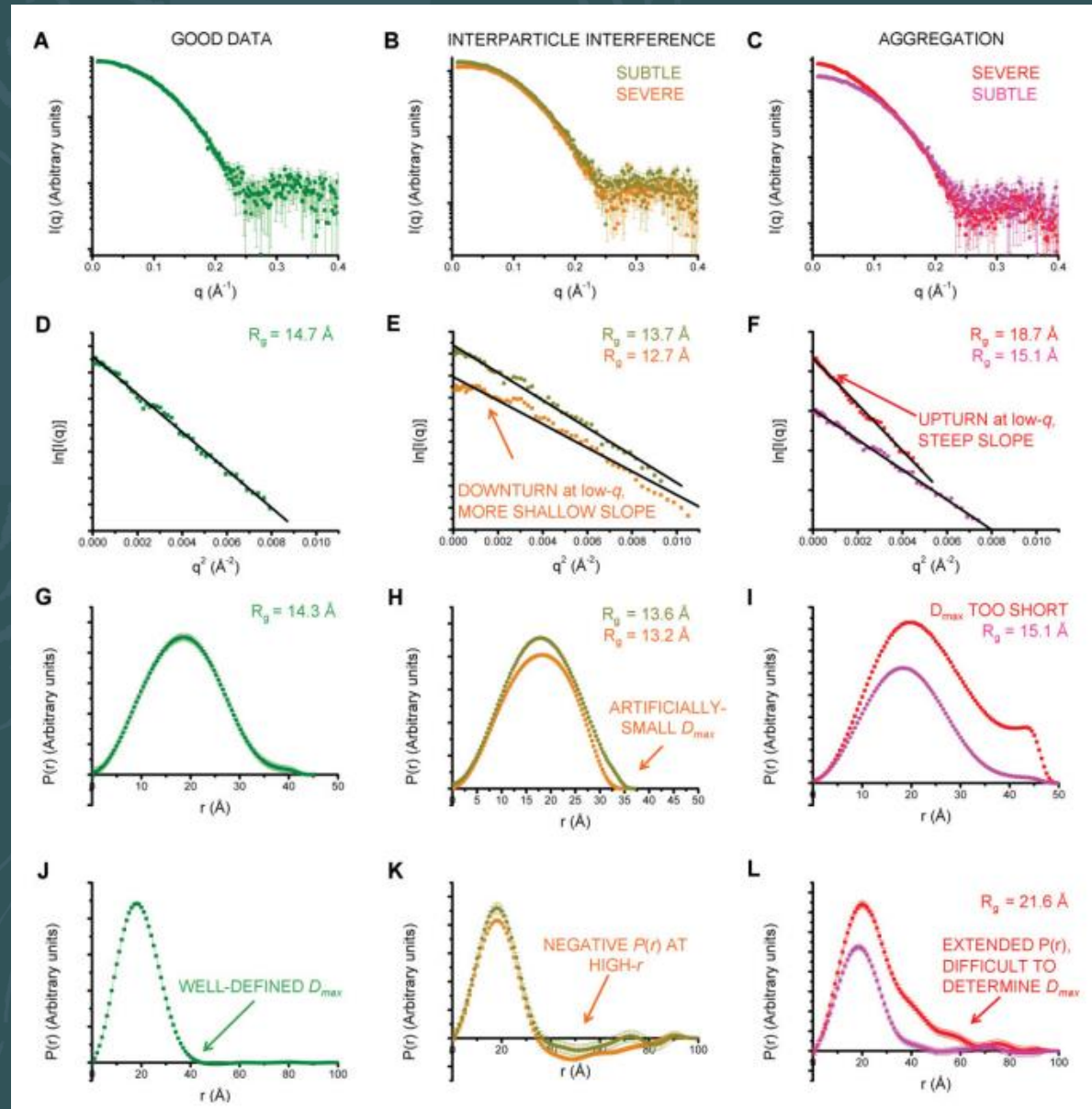
- Obtained data is in the form of $I(q)$ vs q
- This gives information on the shape, but more is needed
- Fourier Transformation
- This gives the function, $P(r)$, the interatomic distance distribution



Data Acquisition

Initial Inspections of Data

- $\log[I(q)]$ vs $\log(q)$
- Guinier Plot
- Behaviour of the $P(r)$ function



A-C: $\log[I(q)]$ vs $\log(q)$ plots

D-F: Guinier Plots

G-L: $P(r)$ Function Plots (J-L have larger x-axis)

Data Acquisition

Standards

- Calibrate $I(0)$ to a scattering standard
- Allows the MW & volume to be obtained from the concentration

Calibration can be done two ways:

1. Comparison with a known particle of similar composition (Protein Standard)
2. An absolute scale using the scattering of water

Recall that:
 $I(0) \propto (\Delta\rho v)^2$

Errors in these values can lead to large MW differences

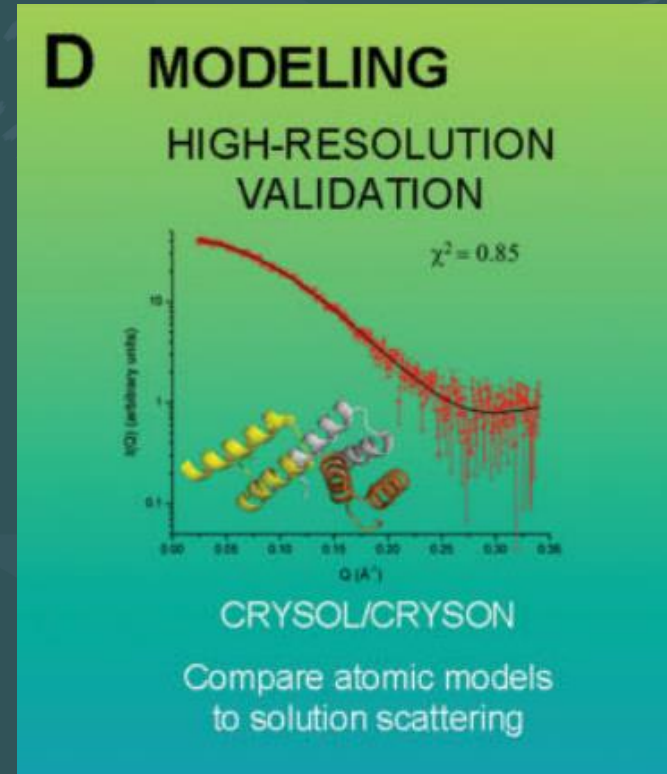
By rearranging an earlier equation, we get:

$$MW = \frac{I(0) * N_A}{C(\Delta\rho v)^2}$$

Modeling

High-Resolution Validation

- Theoretical scattering using programs like CRY SOL
- Atomic models can be obtained using x-ray crystallography or NMR, theoretical models using homology modelling
- "scattering data are significantly challenged in proving any model correct, they can unequivocally prove a model wrong or incomplete"



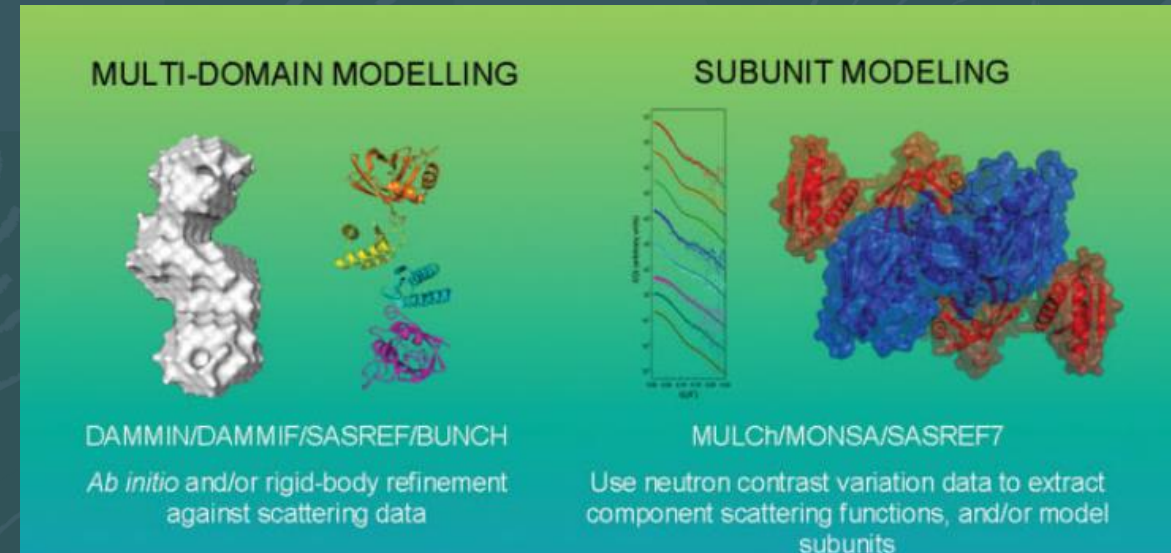
Modeling

Multi-domain Modeling

- Ability to construct a molecular shape from scattering data alone
- Use *ab initio* algorithms to represent a particle by finite volume elements, employ annealing to fit experimental data

Subunit Modeling

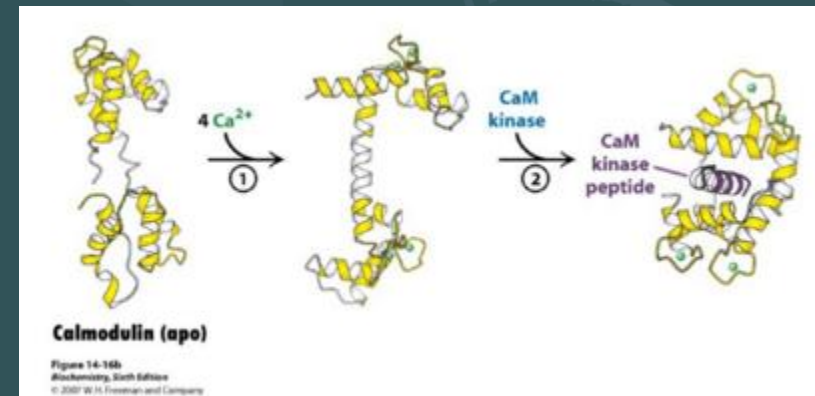
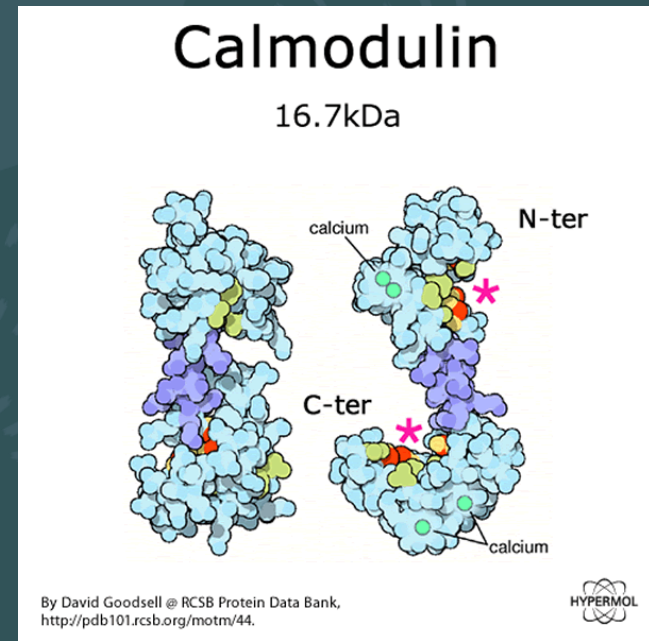
- Used if a conformational change is expected



Modeling

Subunit Modeling Example

- Analyzed the protein, calmodulin
- Found that a dramatic conformational change occurred when it was bound to its target peptide
- Peptide was small enough to not contribute to the scattering profile



Conclusion

SAS experiments must exhibit high standards in quality control and data validation including:

- Detailed reports of data such as the $P(r)$ and Guinier Plots
- Concentration Series
- Normalization of at least one secondary standard

References

- Jacques, D. A., & Trewthella, J. (2010). Small-angle scattering for Structural Biology—expanding the frontier while avoiding the pitfalls. *Protein Science*, 19(4), 642–657.

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Questions?